

INTO YEAR 7...

KNOWLEDGE ORGANISERS



INTO Y7 — MEASUREMENT...

Converting Units

@whisto_maths

What do I need to be able to do?

By the end of this unit you should be able to:

- Recognise metric measures
- Convert metric measures
- Calculate with metric measures
- Understand Miles and Kilometre relationships
- Recognise Imperial measures and conversions

Keywords

Length: the distance from one point to another

Mass: a measure of how much matter is in an object

Capacity: the amount an object can contain (normally liquids)

Volume: the amount of 3-dimensional space an object takes up (units of length cubed)

Convert: to change a value or expression from one value to another.

Imperial: a system of weights and measures originally developed in England

Metric: a system of measuring that replaced the imperial system to fall in line with the rest of Europe.

Proportion: values of two items that increase in the same ratio

Metric measures

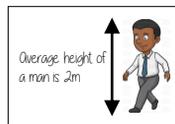
Length Common units of length or distance are

Millimetres (mm) – "Milli" prefix means one thousandth or $\div 1000$

Centimetres (cm) – "Centi" prefix means one hundredth or $\div 100$

Metres (m)

Kilometres (km) – "kilo" prefix means a thousand $\times 1000$



Mass (Weight)

Grams (g)

Kilograms (kg) – "kilo" prefix means a thousand $\times 1000$

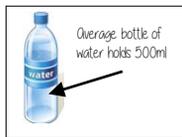
Tonnes (t)



Capacity

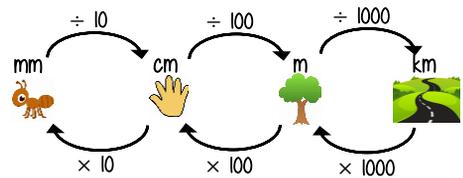
Millilitre (ml) – "Milli" prefix means one thousandth or $\div 1000$

Litre (l)

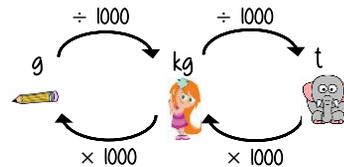


Metric conversions

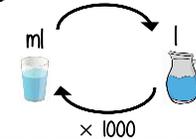
Length



Mass



Capacity



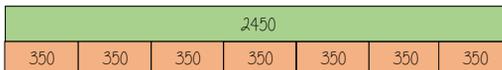
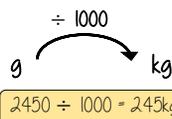
Milli – thousandth
Centi – hundredth
Kilo – thousand

Metric calculations

A package weighs 350g. How much will 7 packages weigh?
Give your answers in kilograms.



The final weight is in grams



Calculations tips:

- Do all calculations in the same unit (often the smaller measurement)
- Read for the units of your answer
- Do all conversions of units at the same time
- Represent your image pictorially where possible

Miles and Kilometres

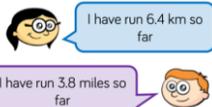
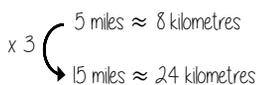
Miles and kilometres are normally used as measures of distance

≈ symbol represents "is approximately equal to"

5 miles ≈ 8 kilometres

Conversion calculations

How many kilometres is 15 miles?



Ron and Onnie are running a 5-mile race.
Who has run the furthest?

5 miles ≈ 8 kilometres $\div 8$
0.625 mile ≈ 1 kilometre $\times 64$
4 miles ≈ 64 kilometre

Ron has 1.2 miles left to run
Onnie has 1 mile left to run
Onnie has run the furthest

Imperial measures

Length

2.5 cm ≈ 1 inch

1 foot = 12 inches

Mass

1 pound (lb) = 16 ounces

1 stone = 14 pounds (lbs)

Capacity

1 gallon = 8 pints



In 1965 Britain converted to the metric system for measurement to fall in line with the rest of Europe. We still use an imperial measurement of miles for distance and speed on our roads.

INTO Y7 — MEASUREMENT ...

Perimeter, Area and Volume

@whisto_maths

What do I need to be able to do?

By the end of this unit you should be able to:

- Display same areas
- Calculate area and perimeter
- Find the area of a triangle
- Find the area of a parallelogram
- Find volume by counting cubes
- Find the volume of a cuboid

Keywords

Area: the size of a surface (2D shapes)

Perimeter: the distance around a 2D shape

Volume: the amount of 3-dimensional space an object takes up (with liquid this is called capacity)

Perpendicular: two lines that meet at 90°

Vertex: a point where two or more line segments meet

Face: any of the flat surfaces of a solid object

Edge: a line segment on the boundary joining one vertex to another

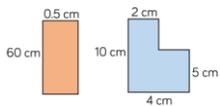
Commutative: you can swap the order around in the calculation and still achieve the same answer

Shapes with the same area

All the shapes have an area of 12cm^2 — they are all made up of 12 squares

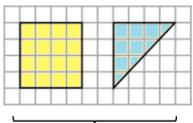


The shapes below also have the same area



Area of triangles

Area can be calculated by counting squares. Often this is an estimation with triangles if it does not cut a square in half.

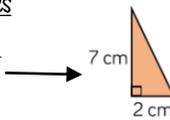


Notice the relationship between the square and the triangle.

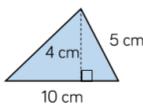
Area triangle = $\frac{1}{2}$ area of the square

Right-angled triangles

The height of a right-angled triangle



Perpendicular heights



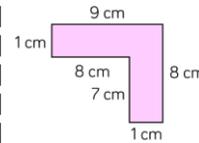
The perpendicular height meets the base at 90°

Area = $\frac{1}{2} \times 10 \times 4 = 20\text{cm}^2$

Area triangle = $\frac{1}{2} \times \text{base} \times \text{perpendicular height}$

Perimeter

Length around the outside of the shape

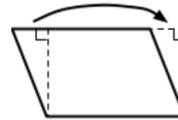


In compound shapes make sure all the lengths have measurements

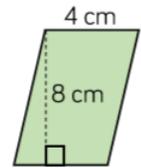
Perimeter = $9\text{cm} + 8\text{cm} + 1\text{cm} + 7\text{cm} + 8\text{cm} + 1\text{cm}$
= 34cm

Perimeter often asks about boundaries or walls in questions

Area of parallelograms



Parallelogram = Base x Perpendicular height

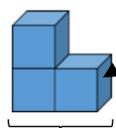


Area = $4 \times 8 = 32\text{cm}^2$

Properties of parallelograms

- Two sets of parallel lines
- Four sides (quadrilateral)
- Interior angles = 360°
- Opposite angles are equal
- 2D shape

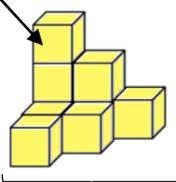
Volume (counting cubes)



Each cube has a given volume. Eg 1cm^3

Always check the units of measurement. Volume can be mm^3 , cm^3 , m^3 , km^3

This shape is made up of 3 cubes. So the volume is 3cm^3



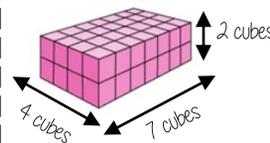
Don't forget about cubes you can't see. This is a 3D shape.

The volume of this shape is 9cm^3



Use multilink cubes to notice that volume can be any shape — it is the number of cubes that make up the value

Volume of cuboids



Counting cubes

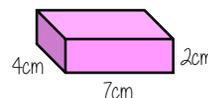
Counting the cubes = 56cm^3

OR

There are 28 cubes on the bottom row and two rows $28 \times 2 = 56$

Volume of cuboid = length x width x height

Volume = $4 \times 7 \times 2 = 56\text{cm}^3$



Properties of cuboids

- 3D shape
- 8 vertices
- 6 faces
- 12 edges

Remember multiplication is commutative so the values can be multiplied in any order

INTO Y7 — NUMBER ...

Ratio

@whisto_maths

What do I need to be able to do?

By the end of this unit you should be able to:

- Use ratio language
- Understand ratios and fractions
- Use the : symbol for ratio
- Calculate ratios
- Use scale factors
- Calculate scale factors
- Link ratio and proportion

Keywords

- Ratio:** a statement of how two numbers compare
- Enlargement:** to change the size of a shape
- Proportion:** a statement that links two ratios
- Scale Factor:** the multiple that increases/ decreases a shape in size
- Part:** a section of a whole
- Scale:** the comparison of something drawn to its actual size
- Order:** to place a number in a determined sequence

Ratio Language

"For every XXX of XXX there are XXX of XXX"

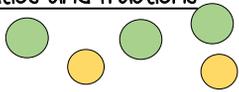


For every 4 cows there are 3 pigs

For every 3 pigs there are 4 cows

Ratios and fractions

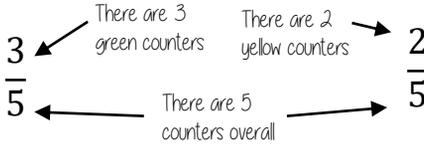
For every 3 green counters there are 2 yellow counters



The ratio of green to yellow counters is $3 : 2$

The fraction of green counters is:

The fraction of yellow counters is:



The ratio symbol



"For every 2 strawberries I have 4 bananas and 6 berries"

Ratio of strawberries, bananas and berries $2 : 4 : 6$



The order of notation follows the order of the parts

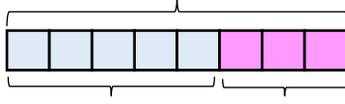


The colon notation is the symbol for ratio "For every..."

Representing a ratio

"For every 5 boys there are 3 girls"

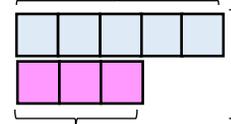
This is the "whole" — boys and girls together



This represents the 5 boys This represents the 3 girls

$5 : 3$

This represents the 5 boys

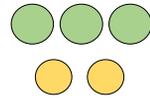


This represents the 3 girls

This is the "whole" — boys and girls together

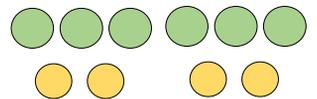
Proportion

The ratio of green to yellow counters is



$3 : 2$

$\frac{3}{5}$ are green $\frac{2}{5}$ are yellow



The ratio of green to yellow counters is

$6 : 4$

$\frac{6}{10} = \frac{3}{5}$ are green
 $\frac{4}{10} = \frac{2}{5}$ are yellow

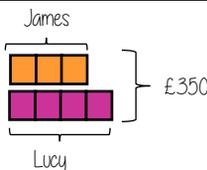
Ratio increases proportionally
The proportion remains the same

Sharing a whole into a given ratio

James and Lucy share £350 in the ratio 3:4. Work out how much each person earns

Model the Question

James: Lucy
 $3 : 4$



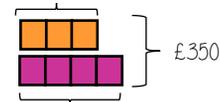
Find the value of one part

Whole: £350
7 parts to share between (3 James, 4 Lucy)

$£350 \div 7 = £50$

□ = one part = £50

James = $3 \times £50 = £150$



Lucy = $4 \times £50 = £200$

Scale Factors

The two rectangles are similar.

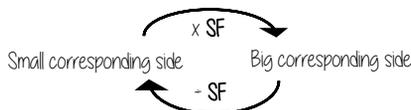


Use corresponding sides to calculate a scale factor

This is an enlargement of scale factor 15

Scale factor can also be calculated by:

Bigger corresponding side
Smaller corresponding side



Ratio increases proportionally
The proportion remains the same

INTO Y7 — GEOMETRY ...

Properties of shape

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What do I need to be able to do?

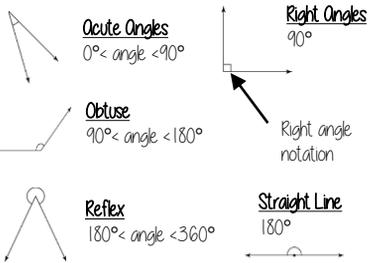
By the end of this unit you should be able to:

- Measure with a protractor
- Classify and calculate angles
- Know and calculate angles in a triangle
- Know properties of angles in special quadrilaterals
- Know properties of angles in regular polygons
- Draw shapes and nets of 3D shapes

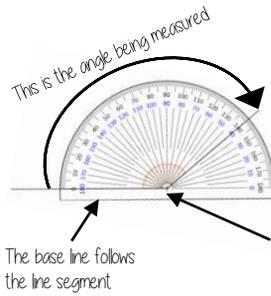
Keywords

- Protractor:** mathematical equipment used to measure angles
Angle: the amount of turn between two lines around their common point
Adjacent: lying next to each other
Sum: addition
Quadrilateral: a four-sided polygon
Polygon: an enclosed 2D shape made up of straight lines
Scalene triangle: a triangle with all different sides and different angles
Regular Polygon: a polygon with equal angles and all sides the same size

Measuring angles



Measure angles to 180°



Read from 0° on the base line. Remember to use estimation. This is an obtuse angle so between 90° and 180°

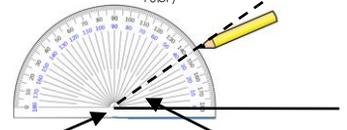
The base line follows the line segment

Make sure the cross is at the point the two lines meet

Draw angles up to 180°

Draw a 35° angle

Make a mark at 35° with a pencil. And join to the angle point (use a ruler)



Make sure the cross is at the end of the line (where you want the angle)

The angle

Angles as measures of turn



Clockwise Anti-Clockwise

East to South is a quarter turn clockwise



Quarter Turn 90°

Clockwise



Half Turn 180°



Three-quarter Turn 270°

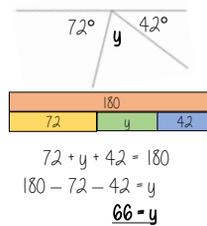
Anti-Clockwise



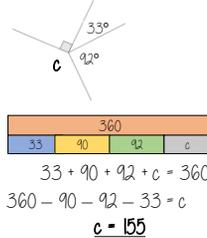
Full Turn 360°

Calculating missing angles

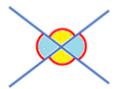
Adjacent angles that share a common point on a line add up to 180°



The sum of angles around a point is 360°



Vertically opposite angles are equal



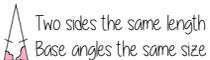
Opposite angles made from straight lines connecting are equal size

Triangles



All interior angles in a triangle add up to 180°

Isoceles Triangles



Two sides the same length
Base angles the same size

Equilateral Triangles



All sides the same length
All angles the same size

Look for combinations of angle rules in triangles. Dash notation indicates equal length sides.

Quadrilaterals



All interior angles in a quadrilateral add up to 360°



Rhombus
All sides equal size
Opposite angles are equal

Kite

No parallel lines
Equal lengths on top sides
Equal lengths on bottom sides
One pair of equal angles



Trapezium
One pair of parallel lines

Polygons

Interior Angles

The angles enclosed by the polygon



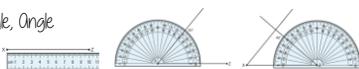
This is an **irregular** polygon — the sides and angles are different sizes

$$(\text{number of sides} - 2) \times 180$$

Remember this is **all** of the interior angles added together

Drawing Triangles

Side, Angle, Angle



Side, Angle, Side



3D shapes and nets

Cube



Cuboid



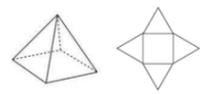
Triangular Prism



Cylinder



Square based pyramid



Vertex: a point where two or more line segments meet
Face: any of the flat surfaces of a solid object
Edge: a line segment on the boundary joining one vertex to another

INTO Y7 — STATISTICS ...

Statistics

@whisto_maths

What do I need to be able to do?

By the end of this unit you should be able to:

- Read and interpret line graphs
- Draw line graphs
- Circles
- Read and interpret pie charts
- Draw pie charts
- The mean

Keywords

Protractor: equipment used to measure and draw angles

Trend: a line on a graph showing the general direction the points seem to follow.

X-axis: the horizontal axis

Y-axis: the vertical axis

Mean: the average of all the numbers

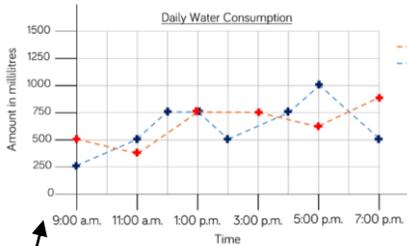
Circumference: the perimeter of a circle. The line around the outside.

Diameter: a straight line that goes through the centre of a circle. The longest line in a circle.

Radius: a straight line from the centre to the radius (Half the length of the diameter)

Line graphs

A method to observe trends in data over time and make comparisons between groups of data.



A key identifies the data set each line represents

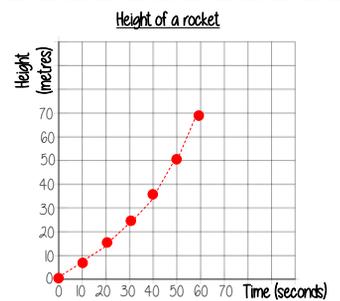
Make comparisons between the data and then relate this information back to the context of the data

"On Tuesday, more water was consumed at 5pm this could have been a period of exercise"

The axes are labelled and show a clear timescale

Drawing line graphs

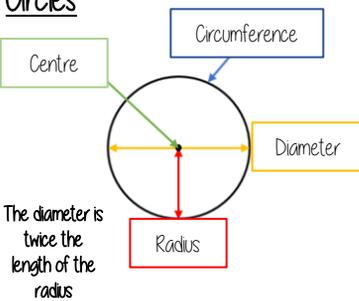
Time (seconds)	Height (metres)
0	0
10	8
20	15
30	25
40	37
50	50
60	70



- Join each point with a straight line.
- Have regular intervals on both axes

Time is labelled across the x axis

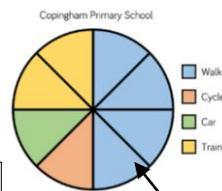
Circles



Read and interpret pie charts

Always read the data for the total amount the pie chart represents

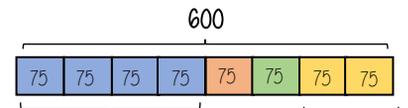
Coppingham Primary School has 600 students



There are 8 equal sectors in this pie chart

There are 360° in a circle

This bar model represents the information in the bar chart



Walking represents half of this data

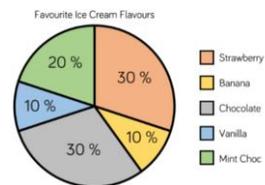
Train represents a quarter of this data

Pie charts with percentages

This survey asked 160 people

The whole pie chart represents 100%

$$10\% = \frac{1}{10} \quad 50\% = \frac{1}{2} \quad 25\% = \frac{1}{4}$$



Strawberry 30% = $\frac{3}{10}$

$160 \div 10 = 16$ ← This is 10% make other calculations from this value
 $16 \times 3 = 48$

Draw pie charts

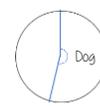
Type of pet	Dog	Cat	Hamster
Frequency	32	25	3

There were 60 people asked in this survey (Total frequency)

$\frac{32}{60}$ "32 out of 60 people had a dog"

This fraction of the 360 degrees represents dogs

$$\frac{32}{60} \times 360 = 192^\circ$$



Multiple method
 As 60 goes into 360 - 6 times
 Each frequency can be multiplied by 6 to find the degrees (proportion of 360)

Use a protractor to draw
 This is 192°

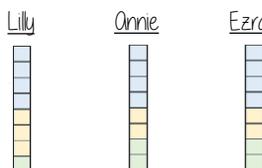
The mean

Mean — a measure of average. It gives an idea of the central value

Lilly, Annie and Ezra have the following cubes



Finding the mean amount is the average amount each person would have if shared out equally



The mean number of blocks would be 8 each

The information is redistributed equally across all groups